

Complete the table of circular function values below for the 5 common angles in the first quadrant and on the positive  $x$ - and  $y$ -axes.

SCORE: \_\_\_\_ / 6 PTS  
(1 POINT DEDUCTED  
FOR EACH ERROR)

$\theta$ (in radians)	$\sin \theta$	$\cos \theta$
0	0	1
$\frac{\pi}{6}$	$\frac{1}{2}$	$\frac{\sqrt{3}}{2}$
$\frac{\pi}{4}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{2}}{2}$
$\frac{\pi}{3}$	$\frac{\sqrt{3}}{2}$	$\frac{1}{2}$
$\frac{\pi}{2}$	1	0

Use the table above to fill in the blanks below. Simplify all answers (including rationalizing denominators). Write "UNDEFINED" if the expression has no value.

SCORE: \_\_\_\_ / 4 PTS

[a]  $\tan \frac{\pi}{2} = \text{UNDEFINED}$      $\frac{\sin \frac{\pi}{2}}{\cos \frac{\pi}{2}} = \frac{1}{0}$

[b]  $\sec 0 = 1$      $\frac{1}{\cos 0} = \frac{1}{1}$

[c]  $\cot \frac{\pi}{3} = \frac{\sqrt{3}}{3}$      $\frac{\cos \frac{\pi}{3}}{\sin \frac{\pi}{3}} = \frac{\frac{1}{2}}{\frac{\sqrt{3}}{2}}$

[d]  $\csc \frac{\pi}{6} = 2$      $\frac{1}{\sin \frac{\pi}{6}} = \frac{1}{\frac{1}{2}}$

Suppose  $\sin t = -\frac{8}{17}$  and  $\cos t = \frac{15}{17}$ . Fill in the blanks below. Simplify all answers.

SCORE: \_\_\_\_ / 4 PTS

[a]  $\sec t = \frac{17}{15}$      $\frac{1}{\cos t} = \frac{1}{\frac{15}{17}}$

[b]  $\sec(-t) = \frac{17}{15}$      $\sec t$

[c]  $\cot t = -\frac{15}{8}$      $\frac{\cos t}{\sin t} = \frac{\frac{15}{17}}{-\frac{8}{17}}$

[d]  $\sin(-t) = -\frac{8}{17}$      $-\sin t$

Fill in the blanks below. Simplify all answers (including rationalizing denominators).  
Write "UNDEFINED" if the expression has no value.

SCORE: \_\_\_\_ / 5 PTS

[a]  $-\frac{19\pi}{6}$  is co-terminal with  $\frac{5}{6}\pi$  (NOTE: Your answer must be between 0 and  $2\pi$ )  $-3\frac{1}{6}\pi + 2(2\pi)$

[b]  $\cos\left(-\frac{19\pi}{6}\right) = -\frac{\sqrt{3}}{2}$  LIKE  $\cos \frac{\pi}{6}$   
BUT NEGATIVE SINCE IN  $Q_2$  (WHERE  $x < 0$ )

[c] The complement of  $\frac{2\pi}{5}$  radians is  $\frac{\pi}{10}$   $\frac{\pi}{2} - \frac{2\pi}{5}$

[d]  $\frac{7\pi}{20}$  radians = 63 degrees  $\frac{7\pi}{20} * \frac{180}{\pi}$

[e] 72 degrees =  $\frac{2\pi}{5}$  radians  $72 * \frac{\pi}{180}$

In the diagram of a central angle on the right,

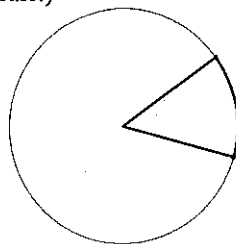
SCORE: \_\_\_\_ / 5 PTS

the radius of the circle is 12 mm and the intercepted arc has length 15 mm. (NOTE: The diagram is **NOT** drawn to scale.)

[a] The central angle is  $\frac{5}{4}$  radians.

$$s = r\theta \rightarrow \theta = \frac{s}{r} = \frac{15\text{mm}}{12\text{mm}}$$

[b] The area of the intercepted sector is  $90\text{mm}^2$ .  $A = \frac{1}{2}r^2\theta = \frac{1}{2}(12\text{mm})^2\left(\frac{5}{4}\right)$



[c] If an object is moving around the circle at a linear speed of 60 mm/s,

its angular speed is  $5$   $\frac{\text{RADIAN}}{\text{SECOND}}$ .  
(specify the units)

$$v = r\omega \rightarrow \omega = \frac{v}{r} = \frac{60\text{mm/s}}{12\text{mm}}$$